

2. (a) Two particles *A* and *B*, of mass 3 kg and 2 kg respectively, are moving in the same direction on a smooth horizontal table when they collide directly. Immediately before the collision, the speed of *A* is 4 m s⁻¹ and the speed of *B* is 1.5 m s⁻¹. In the collision, the particles join to form a single particle *C*.

Find the speed of *C* immediately after the collision.

(3)

- (b) Two particles *P* and *Q* have mass 3 kg and *m* kg respectively. They are moving towards each other in opposite directions on a smooth horizontal table. Each particle has speed 4 m s⁻¹, when they collide directly. In this collision, the direction of motion of each particle is reversed. The speed of *P* immediately after the collision is 2 m s⁻¹ and the speed of *Q* is 1 m s⁻¹. Find

(i) the value of *m*,

(3)

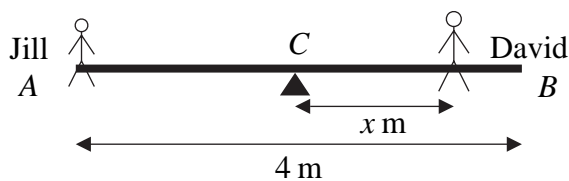
(ii) the magnitude of the impulse exerted on *Q* in the collision.

(2)



3.

Figure 1



A seesaw in a playground consists of a beam AB of length 4 m which is supported by a smooth pivot at its centre C . Jill has mass 25 kg and sits on the end A . David has mass 40 kg and sits at a distance x metres from C , as shown in Figure 1. The beam is initially modelled as a uniform rod. Using this model,

(a) find the value of x for which the seesaw can rest in equilibrium in a horizontal position. **(3)**

(b) State what is implied by the modelling assumption that the beam is uniform. **(1)**

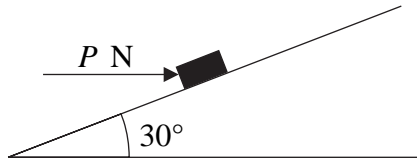
David realises that the beam is not uniform as he finds that he must sit at a distance 1.4 m from C for the seesaw to rest horizontally in equilibrium. The beam is now modelled as a non-uniform rod of mass 15 kg. Using this model,

(c) find the distance of the centre of mass of the beam from C . **(4)**



5.

Figure 2



A parcel of weight 10 N lies on a rough plane inclined at an angle of 30° to the horizontal. A horizontal force of magnitude P newtons acts on the parcel, as shown in Figure 2. The parcel is in equilibrium and on the point of slipping up the plane. The normal reaction of the plane on the parcel is 18 N. The coefficient of friction between the parcel and the plane is μ . Find

(a) the value of P , (4)

(b) the value of μ . (5)

The horizontal force is removed.

(c) Determine whether or not the parcel moves. (5)



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6. [In this question the horizontal unit vectors \mathbf{i} and \mathbf{j} are due east and due north respectively.]

A model boat A moves on a lake with constant velocity $(-\mathbf{i} + 6\mathbf{j}) \text{ m s}^{-1}$. At time $t = 0$, A is at the point with position vector $(2\mathbf{i} - 10\mathbf{j}) \text{ m}$. Find

(a) the speed of A , (2)

(b) the direction in which A is moving, giving your answer as a bearing. (3)

At time $t = 0$, a second boat B is at the point with position vector $(-26\mathbf{i} + 4\mathbf{j}) \text{ m}$.

Given that the velocity of B is $(3\mathbf{i} + 4\mathbf{j}) \text{ m s}^{-1}$,

(c) show that A and B will collide at a point P and find the position vector of P . (5)

Given instead that B has speed 8 m s^{-1} and moves in the direction of the vector $(3\mathbf{i} + 4\mathbf{j})$,

(d) find the distance of B from P when $t = 7 \text{ s}$. (6)



